

# Particle production and chemical freezeout from the hybrid UrQMD approach at NICA energies

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**Abstract.** The energy dependence of various particle ratios is calculated within the Ultra-relativistic Quantum Molecular Dynamics approach and compared with the hadron resonance gas (HRG) model and measurements from various experiments, including RHIC-BES, SPS and AGS. It is found that the UrQMD particle ratios agree well with the experimental results at the RHIC-BES energies. Thus, we have utilized UrQMD in simulating particle ratios at other beam energies down to 3 GeV, which will be accessed at NICA and FAIR future facilities. We observe that the particle ratios for crossover and first-order phase transition, implemented in the hybrid UrQMD v3.4, are nearly indistinguishable, especially at low energies (at large baryon chemical potentials or high density).

## 1 Introduction

One of the main goals of the heavy-ion experiments is the characterization of strongly interacting matter under extreme conditions of high temperature and density [1]. Examining the possible quark-hadron phase transition(s) plays a crucial role in verifying the quantum chromodynamics (QCD), the theory of strong interactions, which predicts that the confined hadrons likely undergo phase transition(s) to partonic matter called quark-gluon plasma (QGP) [2]. So far, various signatures for the QGP formation have been verified, experimentally [3]. The statistical-thermal models [4–11] are successful approaches explaining —among others— the produced particle yields and their ratios. At chemical equilibrium, it is conjectured that the particle ratios are well described by at least two parameters, the baryon chemical potential ( $\mu_b$ ) and the freezeout temperature ( $T_{ch}$ ). The chemical freezeout is defined as a stage during the evolution of the high-energy collision at which the inelastic collisions are assumed to disappear and the number of

produced particle should be fixed. Experiments at the Schwerionensynchrotron (SIS18) [12, 13], the Alternating Gradient Synchrotron (AGS) [5], the Super Proton Synchrotron (SPS) [7], and the Relativistic Heavy-Ion Collider (RHIC) [14–17] have been successfully reproduced within the statistical-thermal approaches [4].

The dependence of both freezeout parameters ( $T_{ch}$  and  $\mu_b$ ) on the nucleon-nucleon center-of-mass energies ( $\sqrt{s_{NN}}$ ) known as the chemical freezeout boundary looks very similar to the QCD phase-diagram separating confined hadrons from deconfined QGP [18]. In lattice QCD simulations [19, 20], which are very reliable at  $\mu_b/T \leq 1$ , *i.e.*,  $\sqrt{s_{NN}}$  greater than top SPS energies, the dependence of  $T_{ch}$  on  $\mu_b$  appears very close to the QCD critical line. At larger  $\mu_b$  (lower energies), both boundaries become distinguishable [21]. In this region, lattice QCD simulations suffer from serious numerical difficulties (the so-called sign problem). Thus, we are left with effective models such as statistical-thermal models and QCD-like approaches including linear-sigma and Nambu–Jona-Lasinio models. So far, there are various phenomenological proposals suggesting universal conditions describing the chemical freezeout boundary. For a recent review, the readers are kindly ad-

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vised to consult ref. [4]. Recently, the possible interrelations among the various freezeout conditions have been derived [21].

While the region of the high temperature and low baryonic density at the QCD phase-diagram are explored by the experiments of the RHIC and the LHC, the region of relatively low and intermediate energy will be covered by the future programs: BES-II at RHIC, Nuclotron-based Ion Collider fAcility (NICA) at the Joint Institute for Nuclear Research (Dubna) and the Facility for Antiproton and Ion Research (FAIR, Germany). At NICA there will be the fixed target experiment BM@N with the beam energy  $E_{kin} = 1\text{--}4.5\text{ A GeV}$  and the collider experiment MPD with the collision energy range  $4 \leq \sqrt{s_{NN}} \leq 11\text{ GeV}$ . At the FAIR, the fixed target experiment CBM with  $E_{kin}$  up to  $11\text{ A GeV}$  (SIS100) will work.

In the present work we utilize the hadron resonance gas (HRG) [21] and the Ultra-relativistic Quantum Molecular Dynamics (UrQMD) v3.4 models [22] in order to estimate various particle ratios at energies ranging from  $\sqrt{s_{NN}}$  from 3 to 19.6 GeV. The freezeout parameters ( $T_{ch}$  and  $\mu_b$ ) are determined from the statistical fit of various particle ratios from UrQMD simulations of Au-Au collisions at  $\sqrt{s_{NN}} = 3, 5, 7.7, 11.5$  and 19.6 GeV. The last three energies are the part of the RHIC beam energy scan program (BES I) and at these energies the experimental values of freezeout parameters are obtained also. A comparison of the simulated and these experimental results is discussed. The convincing agreement between UrQMD simulated and experimental parameters encourages us to extend the study to the other beam energies through UrQMD simulations lower down to 3 GeV, in which the baryon density likely reaches its maximum and shall be covered by NICA and FAIR future facilities.

It is obvious that HRG is an effective statistical model which is only applicable to the produced particles in their final stages of the temporal and spatial evolution of the high-energy collision. Thus, both chiral and deconfinement phase transition(s) cannot be modelled in such statistical approaches, which are based on Hagedorn bootstrap picture [21].

The present paper is organized as follows. Section 2 gives short reviews on both approaches: HRG and UrQMD models. In sect. 3, the energy dependence of various particle ratios (sect. 3.1) and the deduced freezeout parameters (sect. 3.2) are presented. In sect. 4, the conclusions are outlined.

## 2 Approaches

In the present work, the hybrid UrQMD model is used to calculate various particle ratios at energies ranging between 3 and 19.6 GeV. The limitation of this energy range is appropriate as long as the location of the critical endpoint (CEP) is not known yet. CEP widely varies in both  $\mu$ - and  $T$ -dimension. The freezeout parameters: temperature ( $T_{ch}$ ) and baryon chemical potential ( $\mu_b$ ), shall be determined from the statistical fits of various particle ratios from the HRG model to experimental data and to

UrQMD simulations, separately. The latter were generated with first-order or crossover phase transitions. Our UrQMD ensemble contains 10 000 and 150 000 events for high and low energies, respectively.

### 2.1 Hadron Resonance Gas (HRG) model

In grand-canonical ensemble, the partition function of an ideal gas consisting of hadrons and resonances is given as [4]

$$Z(T, V, \mu) = \text{Tr} \left[ \exp \left( \frac{\mu N - H}{T} \right) \right], \quad (1)$$

where  $H$  is the Hamiltonian and  $\mu$  and  $T$  are the chemical potential and the temperature of the system of interest, respectively. The Hamiltonian counts the relevant degrees-of-freedom of confined and strongly interacting medium. Interactions (correlations) can be included implicitly, for instance, in the ones responsible for the resonance formation, *i.e.*, strong interactions. In the HRG model, eq. (1) sums up contributions from a large number of hadron resonances [4] consisting of light and strange quark flavors as listed in the most recent particle data group compilation with masses  $\leq 2\text{ GeV}$  [23]. This corresponds to 388 different states of mesons and baryons besides their anti-particles. More details can be found in ref. [4]. The decay branching ratios are also taken into consideration. For the decay channels with not-yet-measured probabilities, we follow the rules given in ref. [24]. No finite size correction was applied [6];

$$\begin{aligned} \ln Z(T, V, \mu) &= \sum_i \ln Z_i(T, V, \mu) \\ &= \pm \frac{V g_i}{2\pi^2} \int_0^\infty p^2 dp \ln \left[ 1 \pm \lambda_i \exp \left( \frac{-\varepsilon_i(p)}{T} \right) \right], \end{aligned} \quad (2)$$

where  $\pm$  represent fermions and bosons, respectively,  $\varepsilon_i = \sqrt{p^2 + m_i^2}$  is the dispersion relation of the  $i$ -th particle and  $\lambda_i$  is its fugacity factor [4]

$$\lambda_i(T, \mu) = \exp \left( \frac{b_i \mu_b + S_i \mu_S + Q_i \mu_Q}{T} \right), \quad (3)$$

where  $b_i(\mu_b)$ ,  $S_i(\mu_S)$  and  $Q_i(\mu_Q)$  are baryon, strange and charge quantum numbers (their corresponding chemical potentials) of the  $i$ -th hadron, respectively.

The number density of  $i$ -th particle can be derived from the derivative with respect to the chemical potential of the corresponding quantum number. Such a particle can be a *stable* hadron and decay product out of heavy resonances,

$$\begin{aligned} n_i(T, \mu) &= \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp \left[ \frac{\mu_i - \varepsilon_i(p)}{T} \right] \pm 1} \\ &+ \sum_{j \neq i} b_{j \rightarrow i} \frac{g_j}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp \left[ \frac{\mu_j - \varepsilon_j(p)}{T} \right] \pm 1}, \end{aligned} \quad (4)$$

where  $b_{j \rightarrow i}$  is the decay branching ratio of the  $j$ -th hadron resonance into the  $i$ -th stable particle of antiparticle. In a statistical fit of various particle ratios with the UrQMD simulations or with the measurements at different energies,  $T$  and  $\mu_b$  are taken as free parameters. Details about the statistical fit can be taken from refs. [25, 26]. Their resulting values can be related to each other and each of them to the center-of-mass energy ( $\sqrt{s_{NN}}$ ), separately [4].

It is worth emphasizing where or when HRG can be applied. As mentioned, different numerical methods and algorithms seem to fail while trying to reproduce even the well-identified particles (low-lying states, such as pions, kaons and protons) at very low beam energies or equivalently very large baryon chemical potentials. In this energy limit, some particle species cannot be accessed. This is illustrated in sect. 3, especially fig. 4. In general, the HRG model is a very powerful statistical approach. In spite of its simplicity, it has so far a wide range of implications, especially in describing various aspects of the lattice QCD thermodynamics and the particle production in heavy-ion collisions. The latter are limited to the final state, after the chemical freezeout era. All prior eras of the relativistic collision are not accessible by the HRG model. These would be subject to transport approaches. The UrQMD characterizes almost the entire evolution of the colliding system from very early stages up to the particle production, including hydrodynamical evolution and particlization. This *transport* approach will be elaborated in the section that follows.

## 2.2 Ultra-relativistic Quantum Molecular Dynamics (UrQMD) model

The UrQMD event-generator [27] is a well-known simulation approach enabling the characterization of high-energy collisions. It simulates the phase space of such collisions and implements a large set of Monte Carlo solutions for a large number of paired partial differential equations describing the evolution of phase space densities. The UrQMD model simulates the development of the colliding system from a possibly very early stage (depending on the chosen configuration) up to the final state of the particle production. Its large number of unknown parameters could be fixed from experimental results and by theoretical assumptions.

In the present calculations, we use hybrid UrQMD v3.4 [22] which has been tested and gives reasonable results in the energy range from  $E_{lab} = 2\text{--}160$  A GeV in standard parameter calculations. Furthermore, hybrid UrQMD v3.4 provides the possibility to use two types of the phase transition: first-order and crossover. This allows the study of the possible effects of the hadronization processes on the final-state particle production.

For the case of crossover, in hybrid UrQMD v3.4 the equation of state (EoS) for the fluid dynamical evolution is borrowed from the  $SU(3)$  parity doublet model in which quark degrees of freedom besides the thermal contribution of the Polyakov loop are included [28, 29]. This EoS qualitatively agrees with the lattice QCD results at vanish-

ing baryon chemical potential and —most importantly— is conjectured to be applicable at finite baryon chemical potentials, as well. By the end of the hydrodynamical evolution, the active EoS is changed to the one characterizing the hadron gas. Accordingly, it is assured that the active degrees of freedom on both sides of the transition hypersurface are exactly equivalent [28–30].

For the case of a first-order phase transition, in hybrid UrQMD v3.4 the approach proposed in [31] is used. The hadron matter phase is described by a  $\sigma - \omega$ -type model for the nuclear matter part and a bag model is employed for the quark-gluon plasma phase, with a first-order phase transition between both phases.

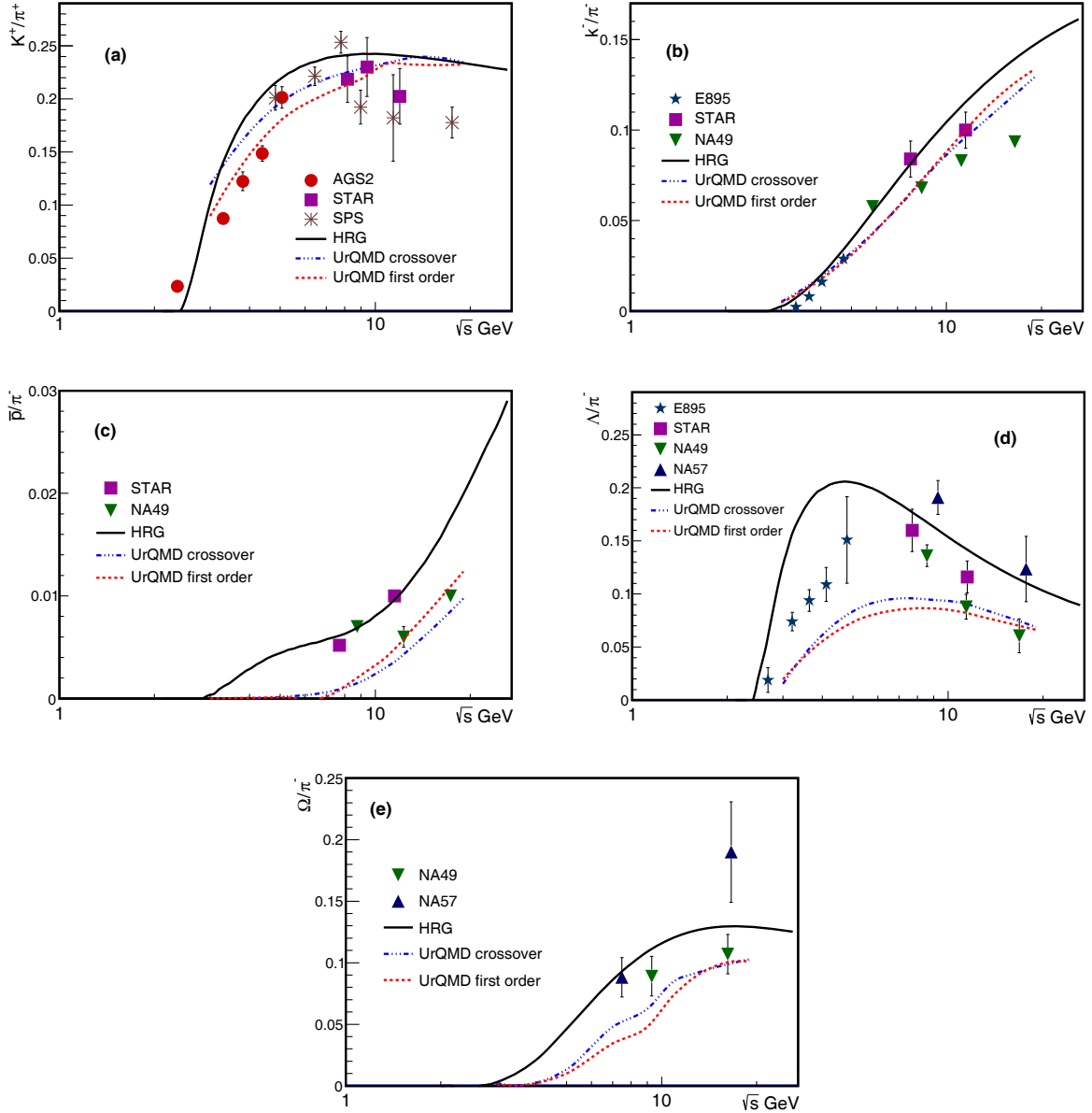
For the sake of completeness, we highlight two differences between crossover and first-order phase transitions, namely the latent heat and the degrees of freedom. In first-order phase transition both are larger than those in the crossover. Furthermore, the crossover takes place smoothly, *i.e.* a relative wide range of temperatures is needed to convert the QCD matter from pure hadron to parton matter or vice versa, while there is a prompt jump in the case of first-order phase transition, *i.e.* the critical temperature becomes relatively sharp [32].

As a limitation, there is some influence of a more technical aspect of UrQMD to its physical outcomes. When the program switches from the hydrodynamical treatment of the high-density stage of the hadronic medium back to the “*normal*” particle-based transport code, there might occur some bias to the resulting particle statistics [33]. Because we selected the same particlization procedure in both cases, the differences of the particle ratios between first-order and crossover phase transition might appear smaller than implied by the physical model.

## 3 Results and discussion

The particles ratios presented in the present work are measured at  $\sqrt{s_{NN}} = 3, 5, 7, 7.7, 9, 11, 11.5, 13, 19$  and  $19.6$  GeV. The beam energies 7.7, 11.5 and 19.6 GeV were part of the STAR BES program. For these energies comparable measurements from experiments of the Superproton synchrotron (SPS), such as NA49, NA44, and NA57 [24], exist. The energy range  $\sqrt{s_{NN}} = 3\text{--}11$  GeV will be covered by the future NICA facility. Thus, it is of great interest to study the particle ratios in both energy regions in experiments and models. If the hybrid UrQMD model can reproduce the STAR results apparently well, further UrQMD simulations at 3 and 5 GeV will be taken as predictions for the future experiments at NICA.

From an ensemble of events created by the hybrid UrQMD model at various beam energies and taking into account two types of the quark-hadron phase transition (crossover and first-order), we shall study the ratios of various particle species in energy dependence. From the statistical fit of the HRG model to the ones simulated with UrQMD and independently to the data from the STAR experiment, both freezeout parameters can be deduced.



**Fig. 1.** The energy dependence of different particle ratios calculated from hybrid UrQMD with first-order (dashed curves) and crossover (triple-dot-dashed curves) phase transition(s) is compared with various measurements:  $K^+/\pi^+$  (a) [34–36],  $K^-/\pi^-$  (b) [34–37],  $\bar{p}/\pi^-$  (c) [34–36,38],  $\Lambda/\pi^-$  (d) [34–37,39–41],  $\Omega/\pi^-$  (e) [34–37,40–42]. The solid curve represents the corresponding calculations from the HRG model.

### 3.1 Energy dependence of various particle ratios

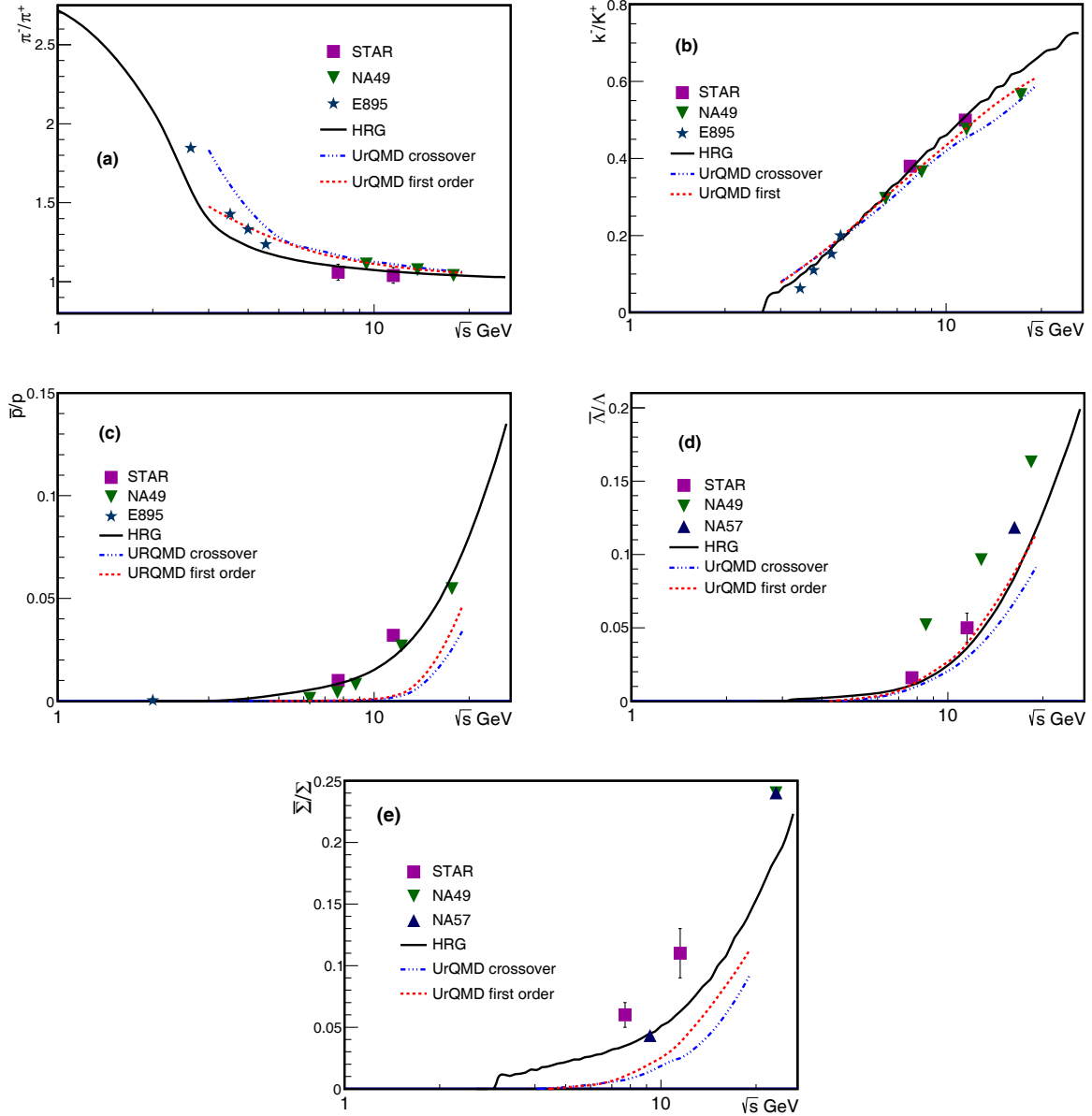
Figure 1 presents the energy dependence of the particle ratios  $K^+/\pi^+$  (a),  $K^-/\pi^-$  (b),  $\bar{p}/\pi^-$  (c),  $\Lambda/\pi^-$  (d) and  $\Omega/\pi^-$  (e). They are generated from the hybrid-UrQMD event generator at various energies and by taking into account two types of the quark-hadron phase transition (crossover (triple-dot-dashed curves) and first-order (dashed curves)). The UrQMD results are compared with measurements (symbols):  $K^+/\pi^+$  (a) [34–36],  $K^-/\pi^-$  (b) [34–37],  $\bar{p}/\pi^-$  (c) [34–36,38],  $\Lambda/\pi^-$  (d) [34–37,39–41],

$\Omega/\pi^-$  (e) [34–37,40–42] and the corresponding calculations from the HRG model.

The HRG particle ratios are determined from eq. (4), in which the baryon chemical potential ( $\mu_b$ ) is replaced by  $\sqrt{s_{NN}}$  [25]

$$\mu_b = \frac{a}{1 + b\sqrt{s_{NN}}}, \quad (5)$$

where  $a = 1.245 \pm 0.094 \text{ GeV}$  and  $b = 0.264 \pm 0.028 \text{ GeV}^{-1}$ . The HRG calculations are in good agreement with both measurements and UrQMD predictions, at least qualitatively. For some of the particle ratios, the agreement is



**Fig. 2.** The same as in fig. 1 but for  $\pi^-/\pi^+$  (a) [34–37],  $K^-/K^+$  (b) [34–37],  $\bar{p}/p$  (c) [34–36,38],  $\bar{\Lambda}/\Lambda$  (d) [34–37,39–41] and  $\bar{\Sigma}/\Sigma$  (e) [43–45].

better than for the other ratios. It should be noticed that these calculations will be fine-tuned in order to reproduce both UrQMD and the experimental results. In doing this, both freezeout parameters will be taken as free variables. Adjusting both the parameters brings HRG calculations to a quantitative agreement with the UrQMD and the experimental results. It is worth noticing that the particle ratios from both types of phase transition are almost indistinguishable, especially at lower energies (larger baryon chemical potentials).

In fig. 2, the energy dependence of UrQMD  $\pi^-/\pi^+$ ,  $K^-/K^+$ ,  $\bar{p}/p$ ,  $\bar{\Lambda}/\Lambda$  and  $\bar{\Sigma}/\Sigma$  are illustrated and compared with HRG calculations and various measured ratios;  $\pi^-/\pi^+$  (a) [34–37],  $K^-/K^+$  (b) [34–37],  $\bar{p}/p$  (c) [34–36,38],

$\bar{\Lambda}/\Lambda$  (d) [34–37,39–41] and  $\bar{\Sigma}/\Sigma$  (e) [43–45]. Again, it is obvious that both orders of the phase transitions implemented in the hybrid UrQMD—at least qualitatively—result in both measured (STAR) and calculated (HRG) particle ratios. Concretely, the particle ratios from crossover phase transition are slightly higher than the ones from the first-order. Furthermore, we observe that the agreement between UrQMD simulations or HRG calculations for these particle-antiparticle ratios and their measurements is fairly convincing, at least qualitatively.

Characterizing the energy dependence of ten particle ratios from simulations, calculations and measurements, and being successful in reproducing, at least qualitatively, both UrQMD predictions and STAR measurements by

**Table 1.** Estimated freezeout parameters,  $T_{\text{ch}}$  and  $\mu_{\text{b}}$  in MeV from the statistical fits of the HRG calculations with the hybrid-UrQMD simulations, in which a crossover phase transition is taken into consideration.

$\sqrt{s_{\text{NN}}}$ [GeV]	$T_{\text{ch}}$ [MeV]	$\mu_{\text{b}}$ [MeV]	$\chi^2/\text{dof}$
3	101	636	6.3/6
5	109.5	599	5.0/6
7.7	132	436	15.5/10
9	132.4	429	9.76/10
11.5	138.1	391	8.95/10
13	140	355	10.47/10
19.6	145	200	8.58/10

means of the statistical-thermal HRG furnish us with a solid argumentation for the attempt to deduce the freezeout parameters from the given data sets. In doing this, we assume that the UrQMD simulations take the position of experiments such as STAR. The determination of the freezeout parameters at the energies covered by STAR BES; 7.7, 11.5 and 19.6 GeV are compatible with the UrQMD simulations with crossover phase transition. The results from the HRG statistical fits well with the STAR BES measurements [46–49] can be summarized as

- at 7.7 GeV,  $T_{\text{ch}} = 141$  MeV and  $\mu_{\text{b}} = 412$  MeV with  $\chi^2/\text{dof} = 11.7/9$ ,
- at 11.5 GeV,  $T_{\text{ch}} = 150$  MeV and  $\mu_{\text{b}} = 312$  MeV with  $\chi^2/\text{dof} = 6.9/9$  and
- at 19.6 GeV,  $T_{\text{ch}} = 153$  MeV and  $\mu_{\text{b}} = 149$  MeV with  $\chi^2/\text{dof} = 7.6/9$ .

The results from the statistical fit of the HRG calculations to the UrQMD simulations at the considered values of the collision energies can be found in table 1. It is obvious that both sets of freezeout parameters are compatible with each other.

### 3.2 Determining freezeout parameters

The study of the energy dependence of various particle ratios paves the way towards determining the freezeout parameters, which are taken as free parameters in the HRG approach, from UrQMD simulations. The statistical fit of the HRG calculations to the UrQMD results is motivated by the excellent agreement between UrQMD and STAR particle ratios at the given RHIC-BES energies. The quality of the statistical fit is measured by minimum  $\chi^2$  and  $q^2$

$$\chi^2 = \sum_i \frac{(R_i^{\text{exp}} - R_i^{\text{theor}})^2}{\sigma_i^2},$$

$$q^2 = \sum_i \frac{(R_i^{\text{exp}} - R_i^{\text{theor}})^2}{(R_i^{\text{theor}})^2}, \quad (6)$$

where  $R_i^{\text{exp}}$  and  $R_i^{\text{theor}}$  are the  $i$ -th measured and calculated particle ratio, respectively, and  $\sigma_i$  represents the error in its measurement. In UrQMD,  $\sigma_i$  is restricted to the statistical errors of each particle ratio.

For the particle ratios  $K^+/\pi^+$ ,  $K^-/\pi^-$ ,  $\pi^-/\pi^+$ ,  $K^-/K^+$ ,  $\Lambda/\pi^-$ ,  $\bar{p}/p$ ,  $\bar{\Lambda}/\Lambda$ ,  $\bar{\Sigma}/\Sigma$ ,  $\bar{p}/\pi^-$  and  $\Omega/\pi^-$  a comparison between the HRG statistical fits (dashed lines) with the UrQMD simulations with a crossover phase transition (solid lines) and that with the STAR measurements [46–49] at 7.7, 11.5 and 19.6 GeV (open symbols) is illustrated in panels (a), (c) and (e) of fig. 3. It is apparent that the ability of hybrid UrQMD to generate the STAR particle ratios increases with the beam energy. This is also reflected in the corresponding  $\chi^2$  per degrees of freedom (dof), table 1. Same observation can be reported from qualities of the HRG statistical fits for both UrQMD and STAR results. The comparison between the hybrid UrQMD simulations and the STAR measurements is illustrated in these three panels in order to argue for further UrQMD simulations at other energies, such as 3, 5, 7, 9, 11, 13 and 19 GeV.

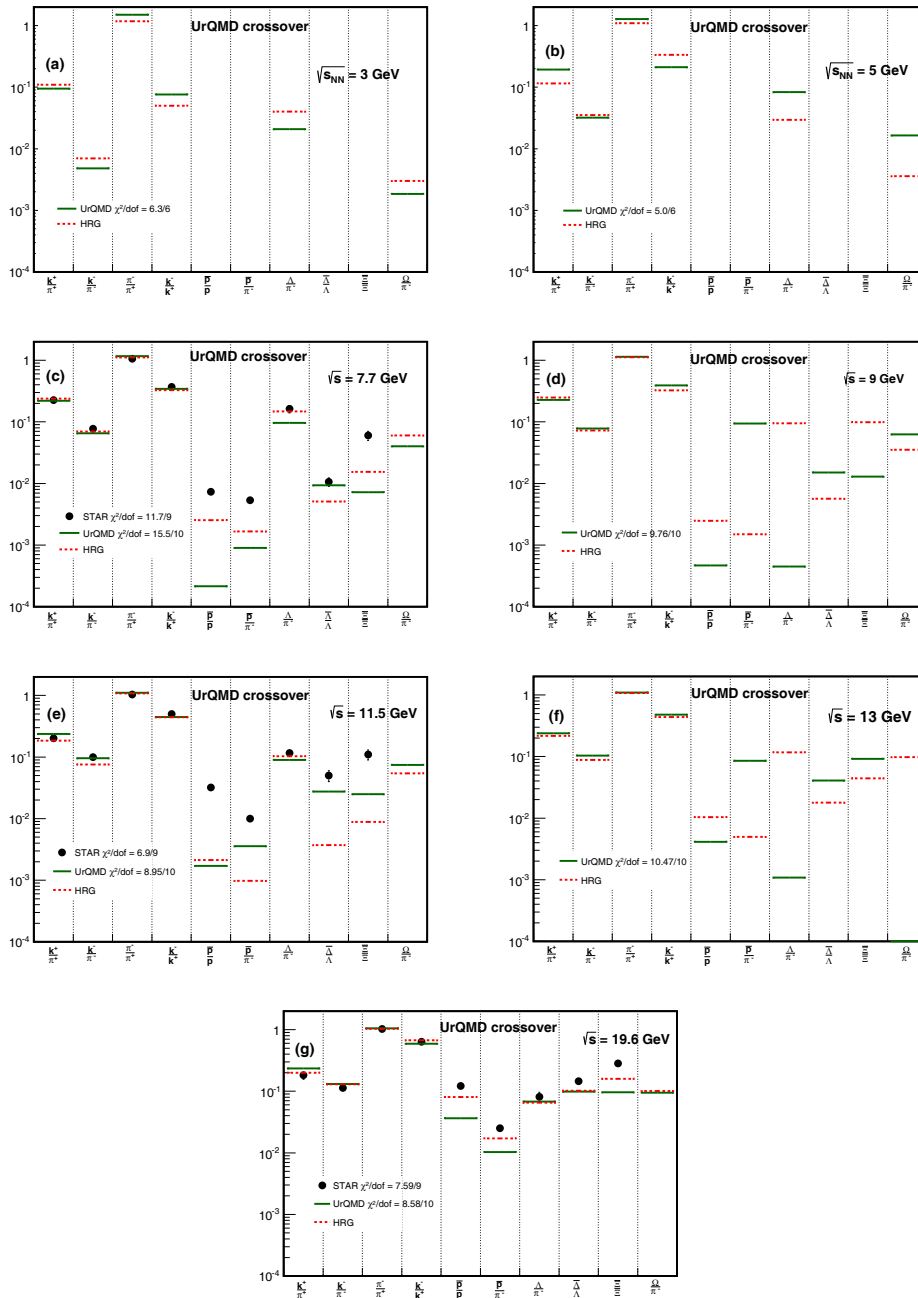
Also, for the crossover phase transition, these ten particle ratios are depicted in panels (b) and (d) as well. Other fits for the first-order phase transition will be illustrated in fig. 4.

The resulting freezeout parameters from the hybrid-UrQMD simulations with crossover and first-order phase transition, tables 1 and 2, respectively, are depicted as a thick-solid curve (crossover) and a dashed curve (first-order phase transitions) in fig. 5. The present calculations are also compared with other estimations (symbols). They are phenomenologically deduced freezeout parameters from measured particle ratios: Cleymans *et al.* [50], Tawfik *et al.* [25,26], HADES [51] and FOPI [52] and from measured higher-order moments of net-proton multiplicity—the  $SU(3)$  Polyakov linear-sigma model (PLSM) and HRG [53]. The thin curve represents the HRG estimations at the freezeout condition  $s/T^3 = 7$ . At a given  $\mu_{\text{b}}$  which is related to beam energy  $\sqrt{s_{\text{NN}}}$ , eq. (5), the freezeout temperature has been determined from the HRG model, sect. 2.1, at which the freezeout condition  $s/T^3 \simeq 7$  is nearly fulfilled.

It is obvious that the UrQMD results agree well with the thermal-model calculations which are based on the higher-order moments of the net-proton multiplicity [53]. Also, the calculations from the  $SU(3)$  PLSM are slightly lower than both UrQMD variants. There is a very small difference between UrQMD with crossover and first-order phase transition as can be determined from tables 1 and 2. Accordingly, we conclude that the resulting freezeout parameters are not affected by the type of the phase transition.

The main reason of the small difference between crossover and first-order transitions could be that in our UrQMD simulations the same value for the particleization criterion was used in both cases. So, influence of this criterion will be the subject for the next investigations.

When we determine the freezeout parameters from the statistical fits of the HRG calculations to the *measured* particle ratios and when we compare them with the fits to UrQMD, we observe that the first ones are relatively higher. This might be due to the assumptions that the constituents of the HRG model are point-like, *i.e.*, no excluded-volume corrections were taken into account,



**Fig. 3.** Assuming crossover phase transition, UrQMD particle ratios (solid lines) are fitted with the HRG calculations (dashed lines): (a) at 7.7, (b) at 9, (c) at 11.5, (d) at 13 and (e) at 19.6 GeV. The resulting freezeout parameters  $T_{\text{ch}}$  and  $\mu_{\text{b}}$  are listed in table 1. The open symbols give STAR BES measurements [46–49]. The smallest  $\chi^2/\text{dof}$  is given in each graph.

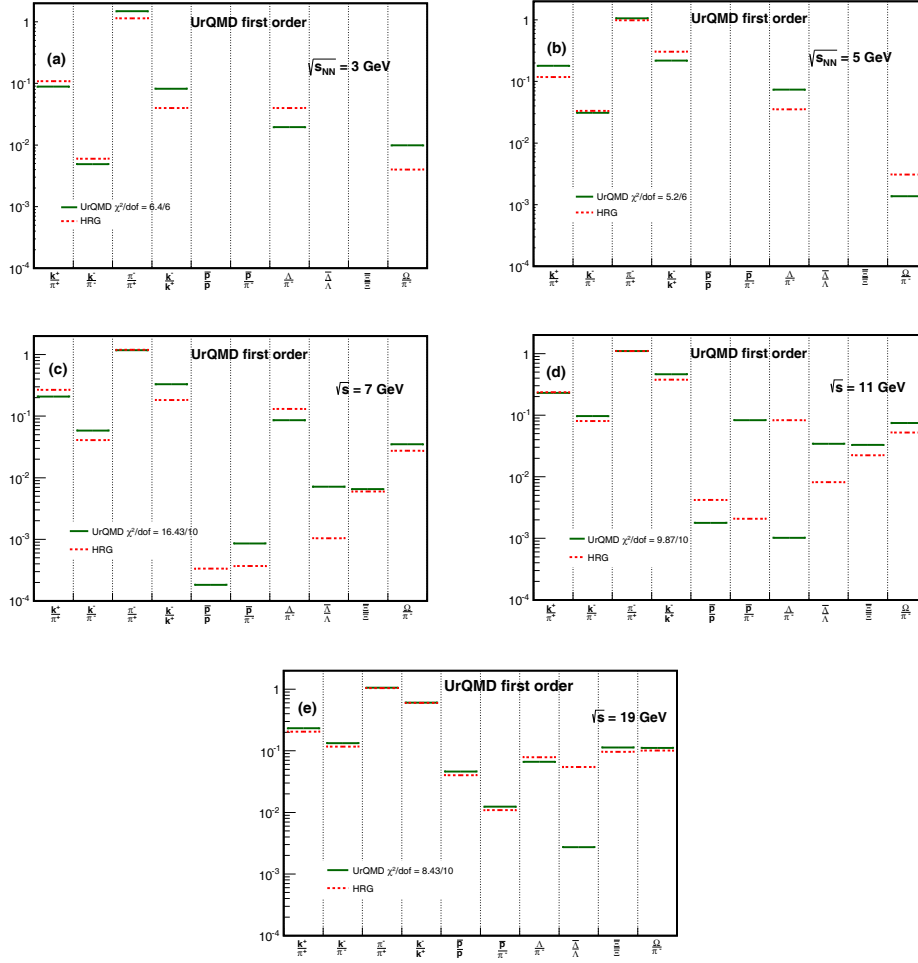
and the quark occupation factors are unity, *i.e.*, light and strange quarks equilibrium, *i.e.*,  $\gamma_f$  factors, where  $f$  runs over the quark flavors, which are multiplied by the quark occupation parameters  $\lambda_i$  in eq. (2). At equilibrium, they are omitted as their values are unity. In nonequilibrium, the quark occupation factors should be stated.

## 4 Conclusion

Ten particle ratios are generated from the hybrid UrQMD v3.4 at different nucleon-nucleon center-of-mass energies.

Two types of the quark-hadron phase transition, crossover and first-order, are taken into consideration. The energy dependence of the resulting particle ratios is compared with the HRG calculations and different measured results from the STAR experiments and from the UrQMD model. Within the energy range considered in this study, a good agreement is observed, at least qualitatively.

We observe that almost all particle ratios from both types of phase transition are nearly indistinguishable, especially at lower energies (larger baryon chemical potentials), which might be interpreted in such a way that the

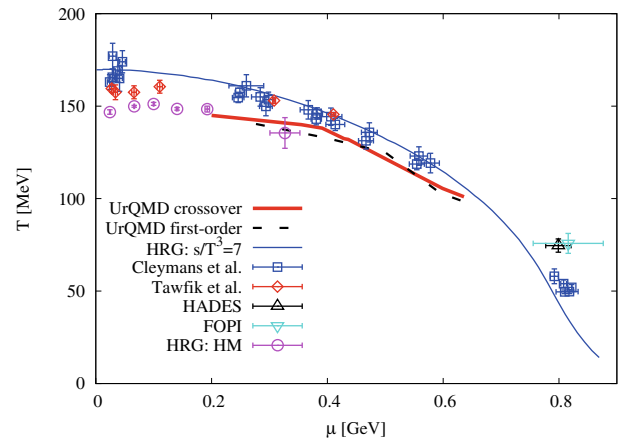


**Fig. 4.** The same as in fig. 3, but here a first-order phase transition is assumed in the hybrid UrQMD simulations at (a) 3, (b) 5, (c) 7, (d) 11 and (e) 19 GeV.

**Table 2.** The same as in table 1 but for hybrid UrQMD simulations with a first-order phase transition.

$\sqrt{s_{NN}}$ [GeV]	$T_{ch}$ [MeV]	$\mu_b$ [MeV]	$\chi^2/dof$
3	99	630	6.4/6
5	103	595	5.2/6
7	125	551	16.43/10
11	133	395	9.87/10
19	142	250	8.43/10

chemical freezeout, at which the particle number should be fixed, apparently takes place immediately after the hadronization process and accordingly the particle production at this chemical equilibrium stage does not differ with respect to its origin. Concretely, we find that for some particle ratios, the simulations with crossover phase transition result in slightly higher temperatures if crossover phase transition is considered than the ones in first-order, and vice versa in other ratios. All particle-to-antiparticle ratios are regularly resulting in slightly higher



**Fig. 5.** The resulting freezeout parameters ( $T$  vs.  $\mu$ ) from hybrid-UrQMD simulations with crossover (solid (short) curve) and first-order phase transition (long-dashed (short) curve) compared with other phenomenological estimations (symbols).

temperatures for crossover phase transition. For these ratios, the agreement between UrQMD or HRG calculations and their measurements is fairly good.



From the energy dependence of the UrQMD particle ratios and the conclusion that the HRG model qualitatively reproduces them and the STAR measurements, as well, we have deduced both freezeout parameters. In doing this, we assume that the UrQMD simulations are experimental inputs. The corresponding uncertainty is determined by statistical errors. We have determined the freezeout parameters at STAR BES, 7.7, 11.5 and 19.6 GeV, whose particle ratios are found compatible with the UrQMD simulations with the crossover phase transition. The resulting freezeout parameters agree well with the ones determined from the statistical-thermal fits of STAR particle ratios at these given energies.

It is found that the resulting freezeout parameters from hybrid UrQMD agree well with the HRG calculations, in which higher-order moments of the net-proton multiplicity are utilized. Furthermore, the freezeout temperatures deduced from the  $SU(3)$  PLSM are slightly lower than the ones from both of them. We conclude that the resulting freezeout parameters are not influenced by the order of the quark-hadron phase transition—or that the aforementioned particlization bias has a possible small influence.

The HRG freezeout parameters determined from the statistical fit of the *measured* particle ratios are relatively higher. This might be understood thanks to the assumption of point-like constituents and equilibrium light- and strange-quarks occupation factors assumed in the HRG model.

Furthermore, the Parton-Hadron-String Dynamics (PHSD) [54] and the Three-Fluid Hydrodynamics (3FH) [55] are conjectured as alternatives to perform much better than UrQMD at low energies, towards the NICA energy range. In a future study, we plan to compare between all these approaches at NICA energies.

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## References

- C.P. Singh, Phys. Rep. **236**, 147 (1993).
- B. Muller, Rep. Prog. Phys. **58**, 611 (1995).
- M. Gyulassy, L. McLarren, Nucl. Phys. A **750**, 30 (2005).
- Abdel Nasser Tawfik, Int. J. Mod. Phys. A **29**, 1430021 (2014).
- P. Braun-Munzinger, J. Stachel, J.P. Wessels, N. Xu, Phys. Lett. B **344**, 43 (1995).
- P. Braun-Munzinger, J. Stachel, J.P. Wessels, N. Xu, Phys. Lett. B **365**, 1 (1996).
- P. Braun-Munzinger, I. Heppe, J. Stachel, Phys. Lett. B **465**, 15 (1999).
- J. Cleymans, H. Satz, Z. Phys. C **57**, 135 (1993).
- S.K. Tiwari, C.P. Singh, Adv. High Energy Phys. **2013**, 805413 (2013).
- J. Rafelski, J. Letessier, Phys. Rev. Lett. **85**, 4695 (2000).
- F. Becattini, J. Cleymans, A. Keranen, E. Suhonen, K. Redlich, Phys. Rev. C **64**, 024901 (2001).
- J. Cleymans, D. Elliott, A. Keranen, E. Suhonen, Phys. Rev. C **57**, 3319 (1998).
- R. Averbeck, R. Holzmann, V. Metag, R.S. Simon, Phys. Rev. C **67**, 024903 (2003).
- STAR Collaboration (J. Adams *et al.*), Nucl. Phys. A **757**, 102 (2005).
- STAR Collaboration (M.M. Aggarwal *et al.*), *An Experimental Exploration of the QCD Phase Diagram: The Search for the Critical Point and the Onset of Deconfinement*, arXiv:1007.2613 [nucl-ex].
- W. Broniowski, A. Baran, W. Florkowski, Acta Phys. Pol. B **33**, 4235 (2002).
- W. Broniowski, W. Florkowski, Phys. Rev. C **65**, 064905 (2002).
- P. Braun-Munzinger, J. Stachel, Nucl. Phys. A **638**, 3 (1998).
- Z. Fodor, S.D. Katz, JHEP **04**, 050 (2004).
- P. deForcrand, O. Philipsen, Nucl. Phys. B **642**, 290 (2002).
- A. Tawfik, M.Y. El-Bakry, D.M. Habashy, M.T. Mohamed, E. Abbas, Int. J. Mod. Phys. E **25**, 1650018 (2016).
- H. Petersen *et al.*, Phys. Rev. C **78**, 044901 (2008).
- K.A. Olive *et al.*, Chin. Phys. C **38**, 1 (2014).
- A. Andronic, P. Braun-Munzinger, J. Stachel, Nucl. Phys. A **772**, 167 (2006).
- Abdel Nasser Tawfik, Ehab Abbas, Phys. Part. Nucl. Lett. **12**, 521 (2015).
- Abdel Nasser Tawfik, M.Y. El-Bakry, D.M. Habashy, M.T. Mohamed, Ehab Abbas, Int. J. Mod. Phys. E **24**, 1550067 (2015).
- S.A. Bass *et al.*, Prog. Part. Nucl. Phys. **41**, 255 (1998).
- Steinheimer, S. Schramm, H. Stocker, Phys. Rev. C **84**, 045208 (2011).
- J. Steinheimer, V. Dexheimer, M. Bleicher, H. Petersen, S. Schramm, H. Stocker, Phys. Rev. C **81**, 044913 (2010).
- Jussi Auvinen, Hannah Petersen, Phys. Rev. C **88**, 064908 (2013).
- D.H. Rischke, Y. Pursun, J.A. Maruhn, Nucl. Phys. A **596**, 717 (1996).
- D. Zschesche, H. Stocker, W. Greiner, Phys. Rev. C **65**, 064902 (2002).
- P. Huovinen, H. Petersen, Eur. Phys. J. A **48**, 171 (2012).
- STAR Collaboration (J. Adams *et al.*), Phys. Rev. Lett. **92**, 112301 (2004).
- NA49 Collaboration (S.V. Afanasiev *et al.*), Phys. Rev. C **66**, 054902 (2002).
- NA49 Collaboration (C. Alt *et al.*), Phys. Rev. C **77**, 024903 (2008).
- E895 Collaboration (J.L. Kaly *et al.*), Phys. Rev. C **68**, 054905 (2003).
- STAR Collaboration (L. Ruan *et al.*), J. Phys. G **31**, S1029 (2005).
- NA49 Collaboration (T. Anticic *et al.*), Phys. Rev. Lett. **93**, 022302 (2004).
- NA49 Collaboration (C. Alt *et al.*), Phys. Rev. C **78**, 034918 (2008).
- E895 Collaboration (C. Pinkenburg *et al.*), Nucl. Phys. A **698**, 495c (2002).
- NA49 Collaboration (C. Alt *et al.*), Phys. Rev. Lett. **94**, 192301 (2005).
- NA49 Collaboration (S.V. Afanasiev *et al.*), Phys. Lett. B **358**, 275 (2002).

44. NA57 Collaboration (F. Antinori *et al.*), Phys. Lett. B **595**, 68 (2004).
45. STAR Collaboration (M.M. Aggarwal *et al.*), Phys. Rev. C **83**, 024901 (2011).
46. STAR Collaboration (L. Kumar), J. Phys. G: Nucl. Part. Phys. **38**, 124145 (2011).
47. STAR Collaboration (S. Das), Nucl. Phys. A. **904**, 891c (2013).
48. STAR Collaboration (X. Zhu), Acta Phys. Pol. B. Proc. Suppl. **5**, 213 (2012).
49. STAR Collaboration (B.I. Abelev *et al.*), Phys. Rev. C **79**, 034909 (2009).
50. J. Cleymans, H. Oeschler, K. Redlich, S. Wheaton, Phys. Rev. C **73**, 034905 (2006).
51. HADES Collaboration (G. Agakishiev *et al.*), Eur. Phys. J. A **47**, 21 (2011).
52. FOPI Collaboration (X. Lopez *et al.*), Phys. Rev. C **76**, 052203 (2007).
53. P. Alba, W. Alberico, R. Bellwied, M. Bluhm, V.M. Sarti, M. Nahrgang, C. Ratti, Phys. Lett. B **738**, 305 (2014).
54. V.P. Konchakovski, W. Cassing, Yu.B. Ivanov, V.D. Toneev, Phys. Rev. C **90**, 014903 (2014).
55. Yu.B. Ivanov, A.A. Soldatov, Phys. Rev. C **91**, 024914 (2015).